



Neutrino Oscillation Phenomenology



Stephen Parke Fermilab June I, 2004

- Solar (I-2) Sector
- Atmospheric (2-3) Sector
- (I-3) Sector
- CP Violation & Mass Hierarchy

Conclusions

Mixing Overview:

flavor

mass

$$|\nu_{\alpha}\rangle = U_{\alpha i}|\nu_{i}\rangle.$$

(using $s_{ij} = \sin \theta_{ij}$ and $c_{ij} = \cos \theta_{ij}$)

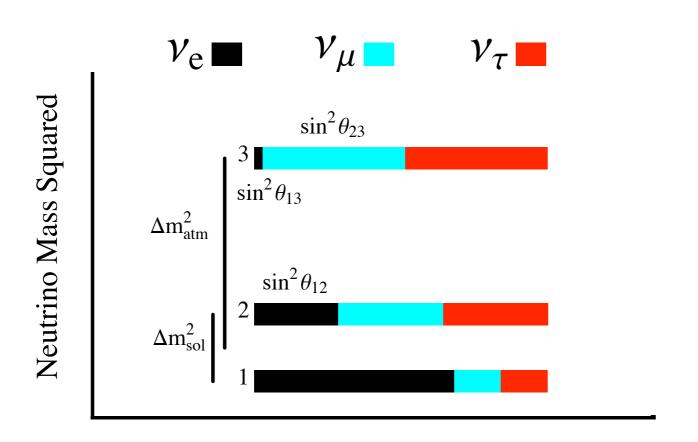
$$U_{\alpha i} = \begin{pmatrix} 1 & & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & & s_{13}e^{-i\delta} \\ & 1 & \\ & -s_{13}e^{i\delta} & & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} \\ & -s_{12} & c_{12} \\ & & 1 \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{i\alpha_2} & \\ & & e^{i\alpha_3} \end{pmatrix}$$

~500 km/GeV

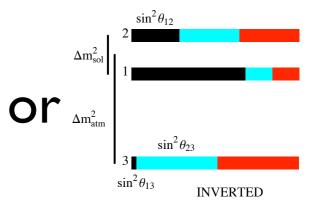
Atmos. L/E $\mu \to \tau$ Atmos. L/E $\mu \leftrightarrow e$ Solar L/E $e \to \mu, \tau$ Majorana

 \sim 18 km/MeV

 $0\nu\beta\beta$



central values θ_{12} , θ_{23} max. for θ_{13} and $|\sin \delta| = 1$



Fractional Flavor Content

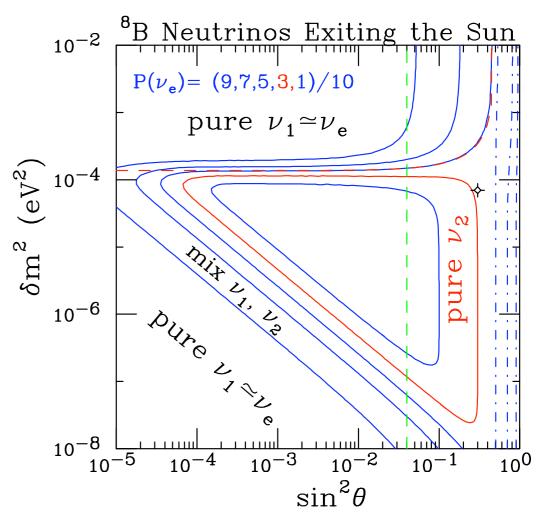
Solar (I-2) Sector:

SNO, KamLAND, SK ...

$$\delta m_{21}^2 = +7.1 \pm 2.0 \times 10^{-5} eV^2$$
$$0.23 < \sin^2 \theta_{12} < 0.35$$

 $\sin^2 \theta_{12} \geq \frac{1}{2}$ excluded at > 5 $\sigma!$ Sign of δm^2_{21} determined at this C.L.

Due to matter effects the $^8{\rm B}$ solar neutrinos exit the sun primarily as ν_2



$$\nu_1 = c_\theta \nu_e + s_\theta \nu_x$$
 $\nu_2 = -s_\theta \nu_e + c_\theta \nu_x$

$$P_{\nu_e} = \frac{1}{2} + \left(\frac{1}{2} - P_x\right) \cos 2\theta_0 \cos 2\theta_N$$

SP. PRL 57,1275(1986)

$$r = N_1/(N_1 + N_2)$$

$$\frac{CC}{NC} = r\cos^2\theta_{12} + (1 - r)\sin^2\theta_{12}$$
$$= \sin^2\theta_{12} + r\cos 2\theta_{12}$$
$$\approx \sin^2\theta_{12}$$

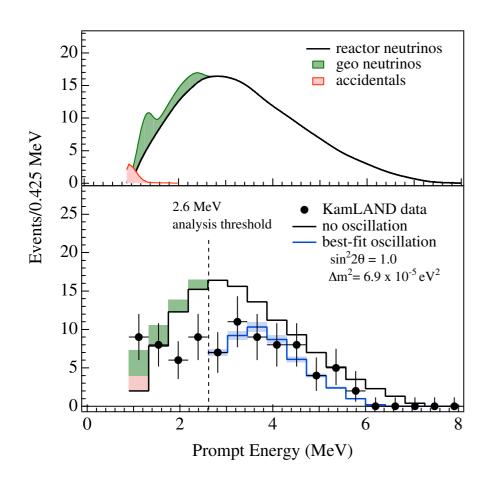
$$0.31 \pm 0.03 \approx 0.29 \pm 0.03$$



Thus SNO's $\frac{CC}{NC}$ is a direct measure of $\sin^2\theta_{12}$.

(Up to small corrections.)

KamLAND Result:

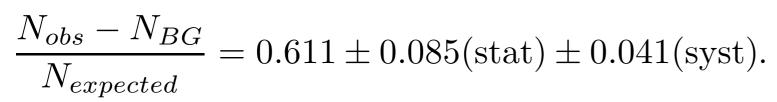


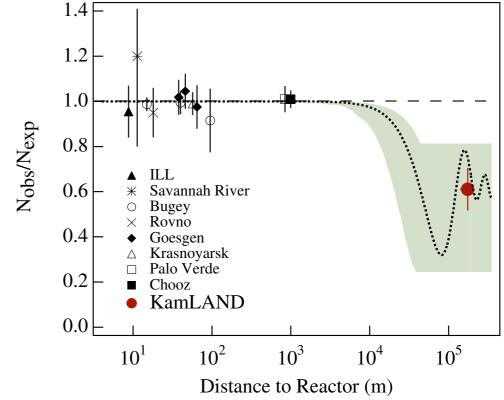
No spectral distortion seen:

$$P(\nu_e \to \nu_e) = 1 - \frac{1}{2}\sin^2 2\theta_{12}$$

Use SNO's $\sin^2 \theta_{12}$

$$=1-2(0.3)(0.7)\approx0.6$$





Atmospheric (2-3) Sector:

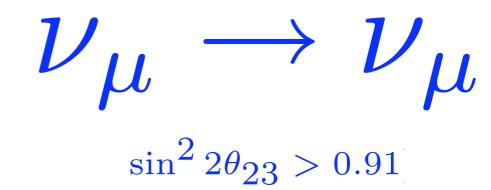
Neutrino Mass Squared

(23)-Sector: SK, K2K

$$|\delta m_{32}^2| = 1.9 - 3.0 \times 10^{-3} \ eV^2$$

$$0.35 < \sin^2 \theta_{23} < 0.65$$

(obtained from $\sin^2 2\theta_{23} > 0.91$)

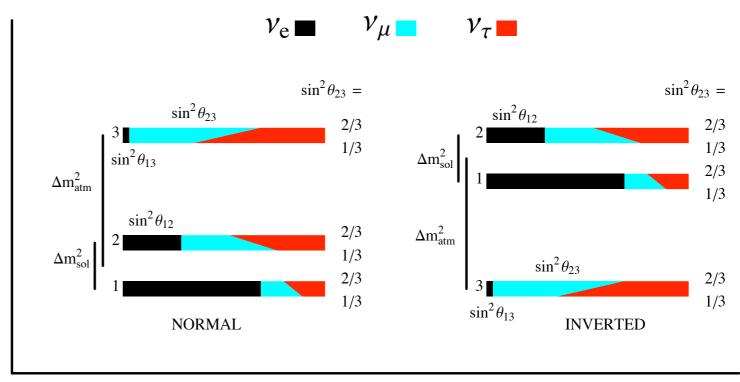


Magnitude of δm_{32}^2 and $\sin^2\theta_{23}$ both poorly known!

Sign of δm_{32}^2 Unknown !!!

MINOS improves on

 $|\delta m_{32}^2|$



Fractional Flavor Content varying $\sin^2 \theta_{23}$

O. Mena and SP hep-ph/0312312

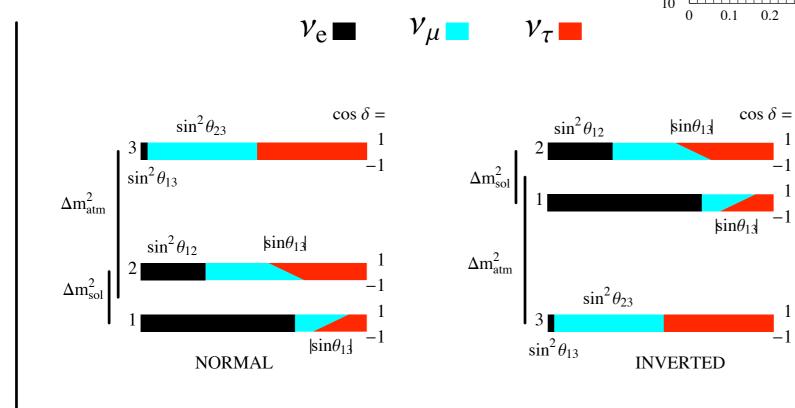
(I-3) Sector:

Chooz, SK and K2K

 $\sin^2 \theta_{13} < 0.03 - 0.05$ limit $|\delta m_{32}^2|$ dependent

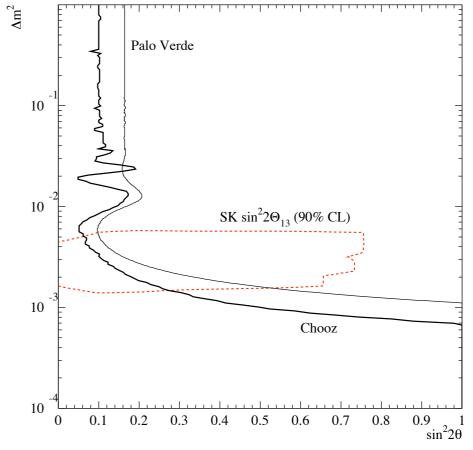
$$0 \le \delta_{CP} < 2\pi$$

Unknown!



Fractional Flavor Content varying $\cos \delta$

Minos to Chooz / 2



Only insensitive to

sign of $\sin \delta$

For $\mu \Leftrightarrow \tau$ symmetry $\theta_{23} = \pi/4$ and $\delta = \pi/2$ or $3\pi/2$ unless $\theta_{13} \equiv 0$

Neutrino Mass Squared

Super-Chooz:

interest in Japan, Europe, Russia, USA (CA and IL), China

$$1 - P_{\nu_e \to \nu_e} = \sin^2 2\theta_{13} \left[\sin^2 \Delta_{atm} + \mathcal{O} \left(\frac{\Delta_{solar}}{\Delta_{atm}} \right) \right] + \mathcal{O} \left(\frac{\Delta_{solar}}{\Delta_{atm}} \right)^2$$
>1%
<3%
<0.1%

kinematical phase

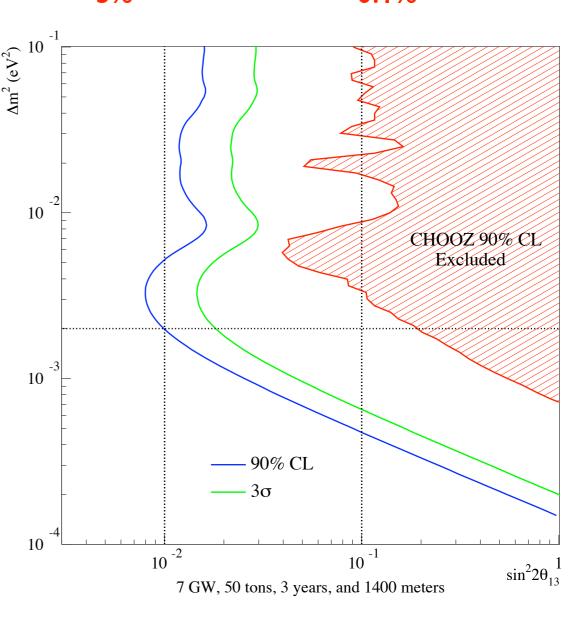
$$\Delta_{atm} = \frac{\delta m_{atm}^2 L}{4E} = 1.27 \frac{\delta m_{atm}^2 L}{E}$$

Clean measurement of

 $\sin^2 2\theta_{13}$ down to 0.01

Systematics limit experiment:

Could be "quick" and "cheap" but ...



J. Link, Columbia

Leptonic CP and T Violation in Oscillations

 $u_{\mu} \leftrightarrow \nu_{e} \qquad \Longleftrightarrow \qquad \bar{\nu}_{\mu} \leftrightarrow \bar{\nu}_{e} \qquad \qquad \mathsf{Super-Beams}$

 $\nu_e \leftrightarrow \nu_\mu \qquad \Longleftrightarrow \qquad \bar{\nu}_e \leftrightarrow \bar{\nu}_\mu$

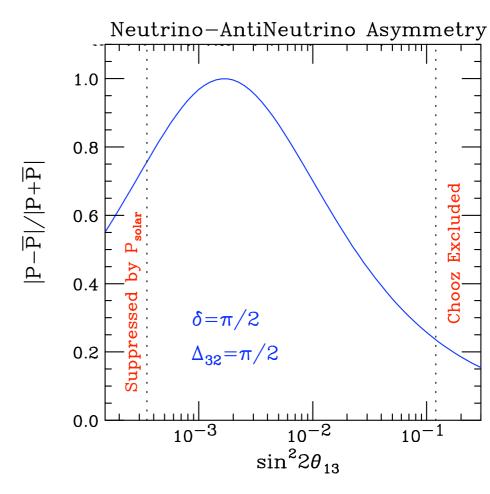
Nu-Factory

 $P_{\nu_{\mu} \to \nu_{e}} = |a_{\mu \to e}^{atm} + a_{\mu \to e}^{sol}|^{2}$

CP Violation comes from the Difference in the Interference of $a_{\mu \to e}^{atm}$ amd $a_{\mu \to e}^{sol}$ for neutrinos verses anti-neutrinos.

CAN BE LARGE!!!.

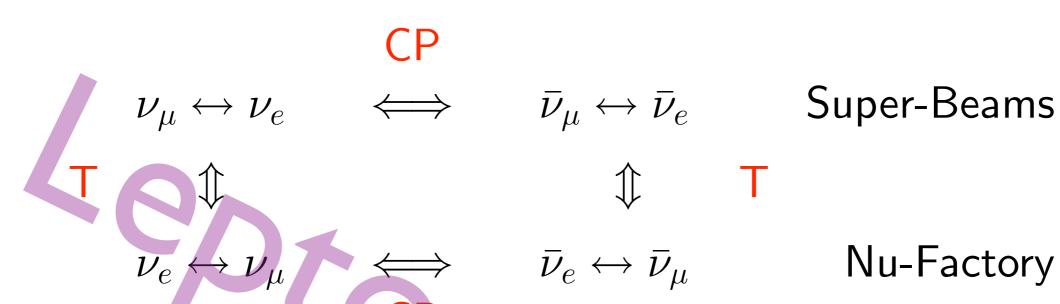
Important parameters are θ_{13} and δ .



kinematical phase

$$\Delta_{ij} = \frac{\delta m_{ij}^2 L}{4E} = 1.27 \frac{\delta m_{ij}^2 L}{E}$$

Leptonic CP and T Violation in Oscillations

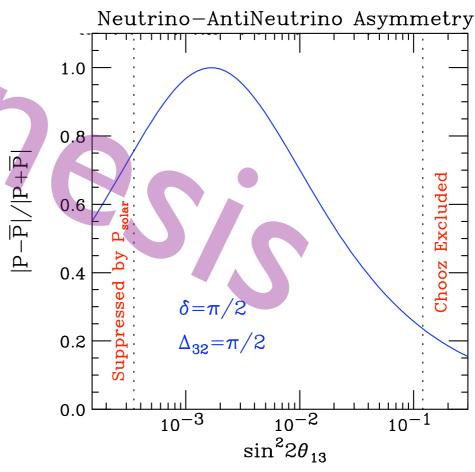


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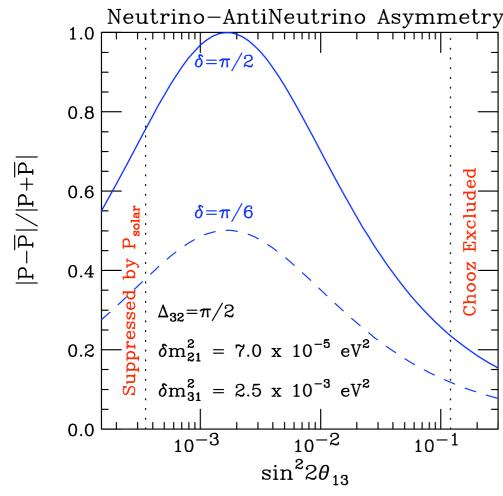
$$\Delta_{ij} = \frac{\delta m_{ij}^2 L}{4E} = 1.27 \frac{\delta m_{ij}^2 L}{E}$$

$$P^{atm}(\nu_{\mu} \to \nu_{e}) = |a^{atm}|^{2} = \sin^{2}\theta_{23}\sin^{2}2\theta_{13}\sin^{2}\Delta_{31}$$

$$P^{sol}(\nu_{\mu} \to \nu_{e}) = |a^{sol}|^{2} = \cos^{2}\theta_{23}\cos^{2}\theta_{13}\sin^{2}2\theta_{12}\sin^{2}\Delta_{21}$$

relative phase is $\Delta_{32} \pm \delta$

$$P(\nu_{\mu} \to \nu_{e}) = |a^{atm} + a^{sol}|^{2} = P^{atm} + P^{sol} + 2\sqrt{P^{atm} \cdot P^{sol}} \cos(\Delta_{32} \pm \delta)$$

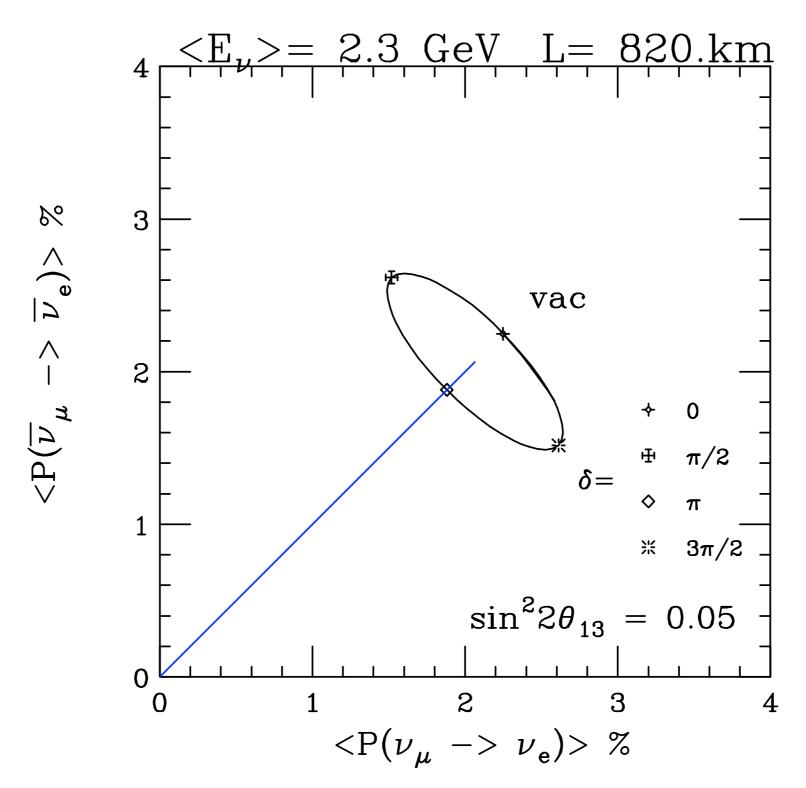


Maximum Asymmetry when

$$|a^{atm}| = |a^{sol}|$$

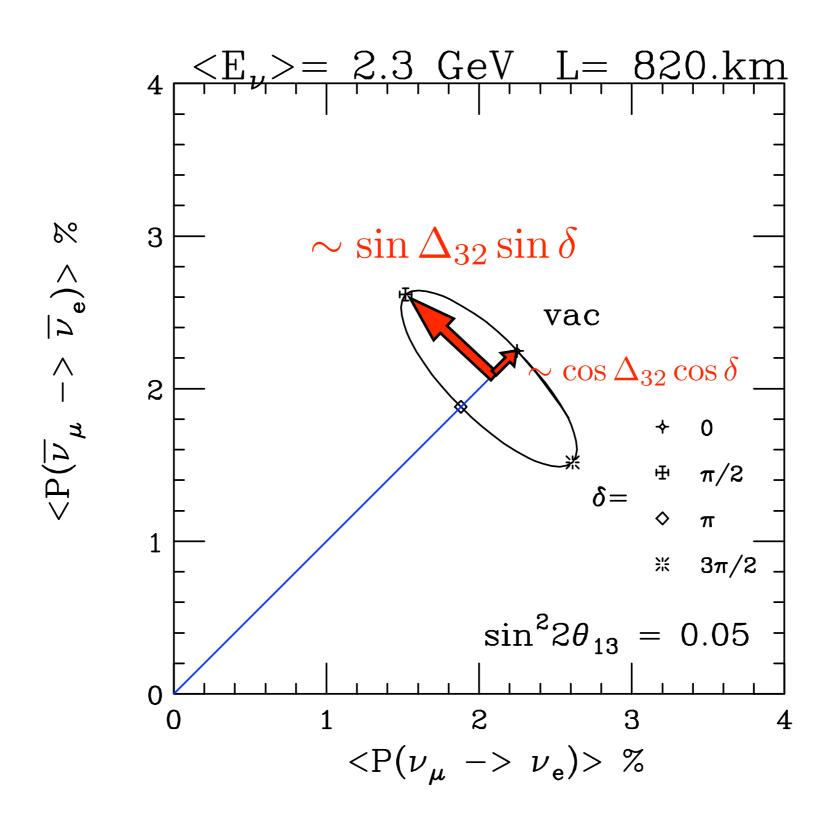
$$\sin^2 2\theta_{13} \approx \frac{\sin^2 2\theta_{12}}{\tan^2 \theta_{23}} \left[\frac{\pi}{2} \frac{\delta m_{21}^2}{\delta m_{31}^2} \right]^2$$

$$\approx 0.002$$



Bi-Probability Plots:

 $\begin{array}{c} \mbox{Minakata and Nunokawa} \\ \mbox{hep-ph/}0108085 \end{array}$

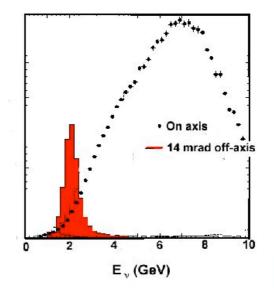


Bi-Probability Plots:

 $\begin{array}{c} {\rm Minakata~and~Nunokawa} \\ {\rm hep-ph/0108085} \end{array}$

Off-Axis Beams:

BNL 1994



The NUMI Beamline





- 295 km baseline
- Super-Kamiokande:
 - 22.5 kton fiducial
 - Excellent e/μ ID
- Additional π⁰/e ID
- Hyper-Kamiokande
 20× fiducial mass of
 - 20× fiducial mass of SuperK
- Matter effects small
- Study using fully simulated and reconstructed data

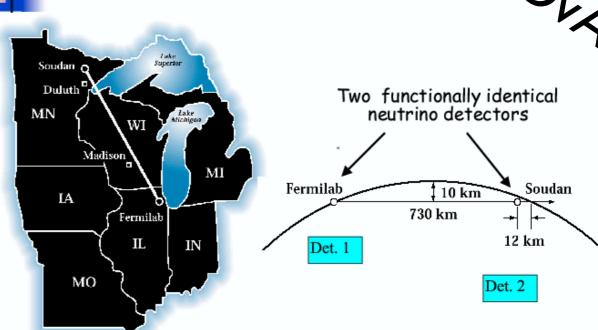


L=295 km and

Energy at Vac. Osc. Max. (vom)

$$E_{vom} = 0.6 \ GeV \left\{ \frac{\delta m_{32}^2}{2.5 \times 10^{-3} \ eV^2} \right\}$$

0.75 upgrade to 4 MW



L=700 - 1000 km and

Energy near 2 GeV

$$E_{vom} = 1.8 \ GeV \left\{ \frac{\delta m_{32}^2}{2.5 \times 10^{-3} \ eV^2} \right\} \times \left\{ \frac{L}{820 \ km} \right\}$$

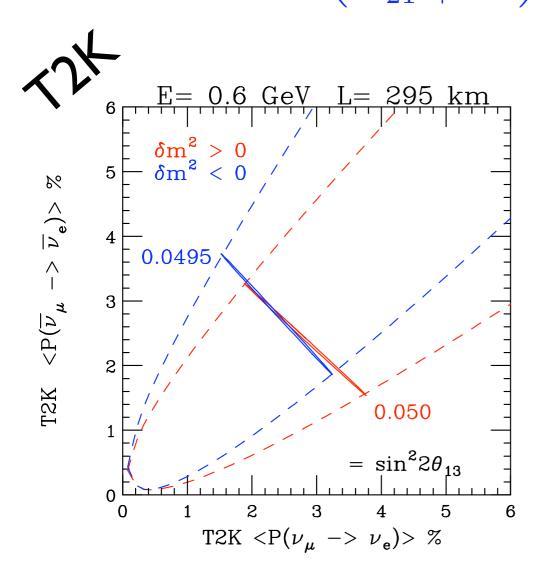
0.4 upgrade to 2 MW

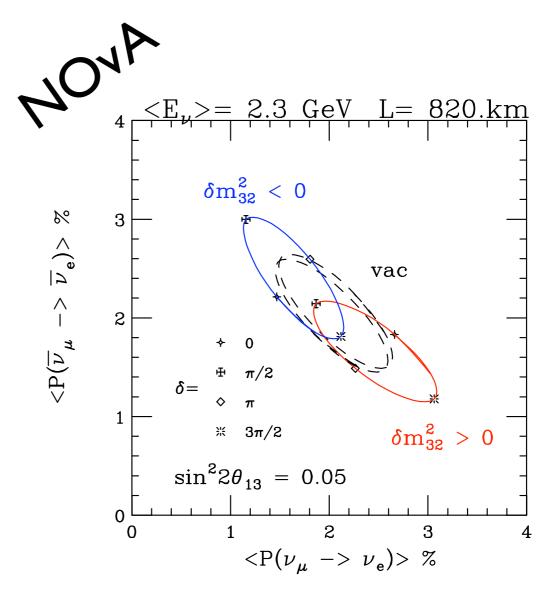
Matter Effects:

$$a = G_F N_e / \sqrt{2} = (4000 \ km)^{-1}$$

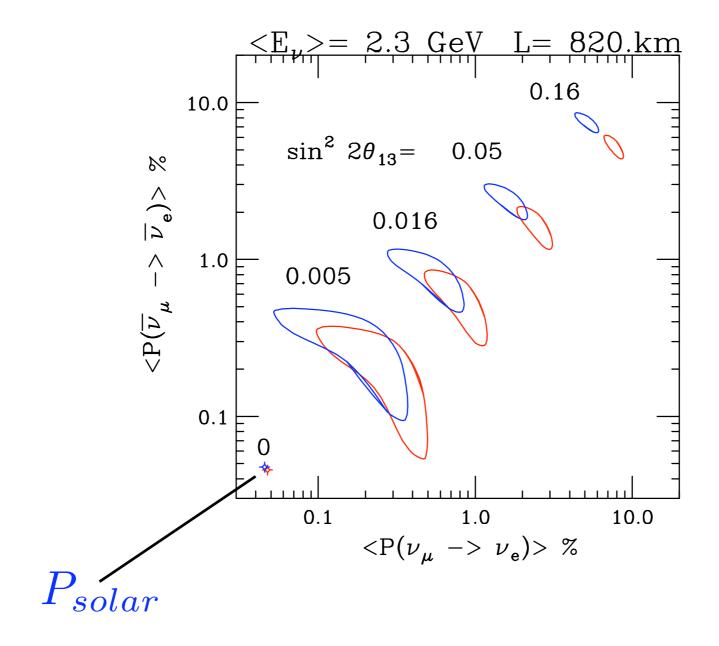
$$\sin \Delta_{31} \implies \left(\frac{\Delta_{31}}{\Delta_{31} \mp aL}\right) \sin(\Delta_{31} \mp aL)$$

$$\sin \Delta_{21} \implies \left(\frac{\Delta_{21}}{\Delta_{21} \mp aL}\right) \sin(\Delta_{21} \mp aL) \approx \Delta_{21}$$





Varying $\sin^2 2\theta_{13}$ Log scale:



Two Signs:

 $sign of \delta m_{31}^2$

normal v inverted hierarchy

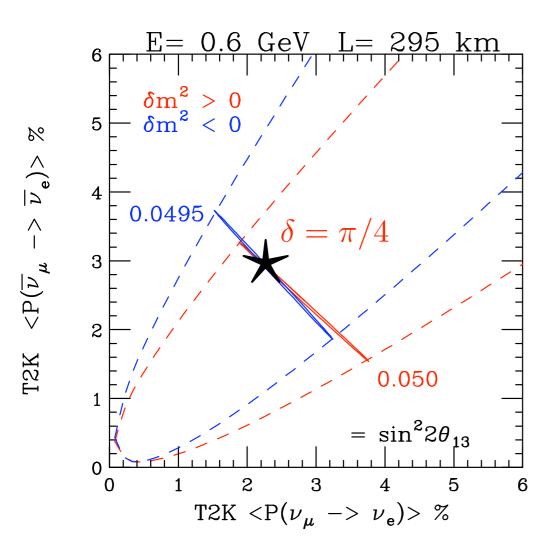
and

Leptonic CP Violation



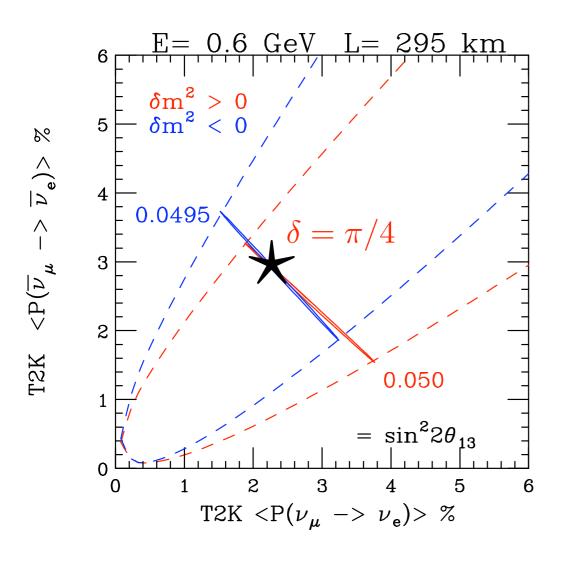
O. Mena and SP

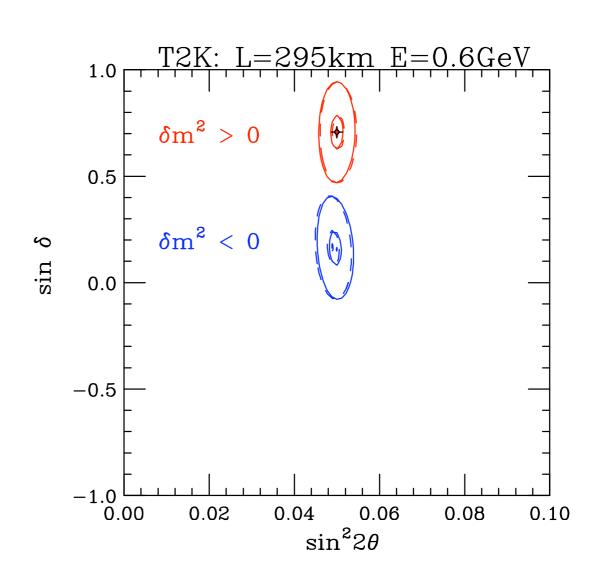
T2K:



T2K:

$$\sin \delta_{+} = \sin \delta_{-} + 0.5\sqrt{\frac{\sin^{2} 2\theta_{13}}{0.05}}$$

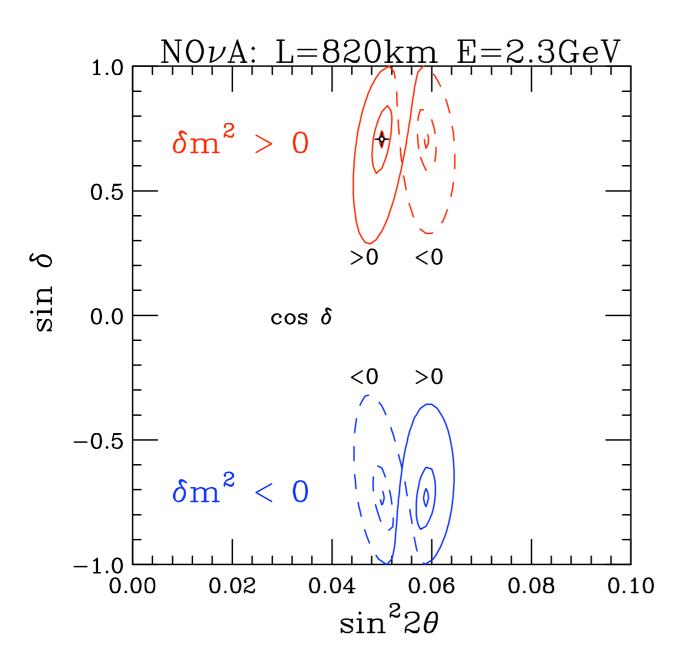


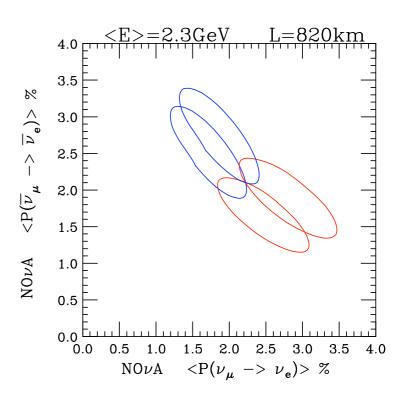


no info on sign of $\cos \delta = \pm \sqrt{1 - \sin^2 \delta}$

NOvA:

$$\sin \delta_{+} = \sin \delta_{-} + 1.5\sqrt{\frac{\sin^2 2\theta_{13}}{0.05}}$$

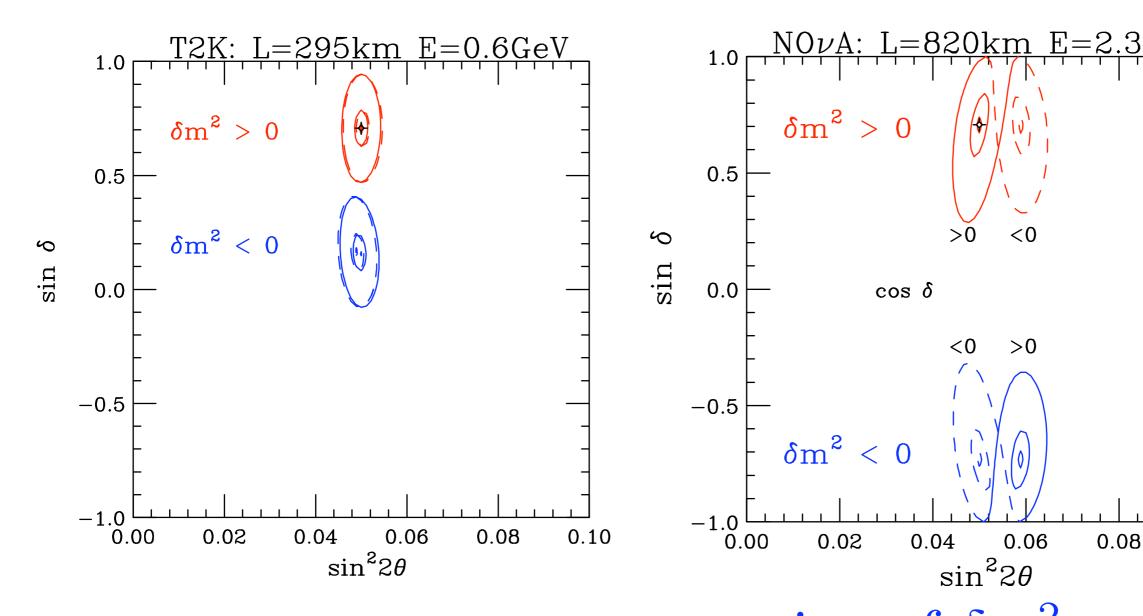




sensitive to sign of

$$\cos \delta = \pm \sqrt{1 - \sin^2 \delta}$$

T2K + NOvA



with sufficient events
T2K plus NOvA determines

sign of δm_{31}^2 =hierarchy

0.10

Hierarchy: T2K Nu v. NOvA Nu

sign δm_{32}^2

At Vac. Osc. Max., $\Delta_{32} = \frac{\pi}{2}$

$$P_{mat} = \left(1 \pm 2 \frac{E}{E_R}\right) P_{vac}$$
 where $E_R \simeq 12$ GeV.

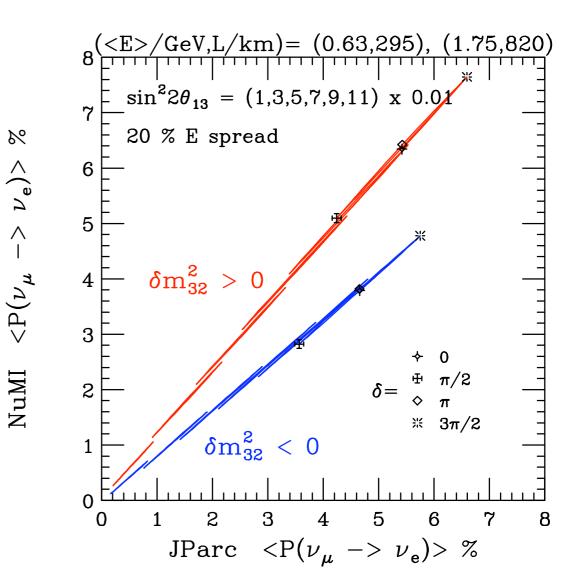
Therefore, if NuMI and JParc both run Neutrinos at Vac. Osc. Max.

$$P_N = \left(1 \pm 2 \frac{(E^N - E^J)}{E_R}\right) P_J$$

i.e.
$$P_N \approx (1.2 \text{ or } 0.8)P_J$$

Need about 100 events in each expt.

(signal)



Separation degraded for $E^N > E_{vom}$.

Minakata, Nunokawa and SP – hep-ph/0301210

Conclusions:

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• \sin^2 2\theta_{13}: Can be measured by Reactor Exp.(\sim 0.01), Long Baseline Exp.(\sim 0.005), Nu Factories (\sim 10^{-4}).
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- sign of δm_{31}^2 and $\sin \delta$: \Rightarrow Mass Hierarchy and CP Violation. $\nu_{\mu} \rightarrow \nu_{e}$ Superbeam Long Baseline Exp. running BOTH ν and $\bar{\nu}$.
- θ_{23} : To break the $\theta_{23} \leftrightarrow \frac{\pi}{2} \theta_{23}$ degeneracy. Combination of Reactor and Long Baseline Exps. $\sin^2 2\theta_{13}$ v. $2\sin^2 \theta_{23}\sin^2 2\theta_{13}$.

sparkE HQ&L 04 24

If the size of θ_{13} is in range of the LBL/Reactor expts, $\sin^2 2\theta_{13} \geq 0.005$, then a few carefully choosen counting experiments with sufficient statistics can determine

$$heta_{13}, \quad \delta_{CP}, \quad ext{sign of } \delta m_{31}^2, \quad heta_{23}.$$

A Fabulous Opportunity in the Neutrino Osc. Sector!!!

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Leaving the Questions of:

Majorana v Dirac?,

Steriles? and

Absolute Mass Scale, M_{lite}?
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